Smooth MT Transfer Function Estimation by An Inverse Scheme

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ABSTRACT

The geophysical exploration of geothermal areas strongly relies upon Magnetotellurics (MT) method, that exploits the measurement of the low-power natural EM field at the Earth's surface. Through the estimation of the MT transfer functions (TF), relating the electric to the magnetic field, the subsurface resistivity distribution can be inferred. Due to the diffusive nature of the low-frequency EM field, the MT TF's are inherently smooth, and smoothness is the main criterion adopted by EM community to assess the estimation quality. In the presence of Gaussian noise, the frequency-domain the least squares (LSQ) method provides the best possible estimate; natural MT data, however, contains a significant amount of non-stationary data that constitute outliers for the LSQ procedure. These outliers make the TF's sharp at several frequencies, according to the nature of the noise. In order to circumvent this problem, robust methods were introduced, and provide a smooth TF, if non-stationarity is a minor fraction of the record. However, as geothermal development proceeds on a global scale, investigations can involve densely populated and industrialised areas. In these zones, high-power artificial is more likely present. Since these disturbance signals can by persistent, robust methods can fail; moreover, preliminary filtering can be ineffective. In these conditions, the applicability of MT is severely hampered.

In some cases, smoothness is a-posteriori introduced by splines or smoothing procedures, but this approach lacks physical consistency. It can also be part of estimation methods but implying the adoption of some arbitrary assumptions. Here we propose a new heuristic algorithm to reach the maximum TF's smoothness through an inverse scheme applied to event rejection in frequency-domain. The algorithm searches for frequency-dependent power thresholds to be applied to the events, in order to achieve the maximum smoothness in the TF's. The smoothness is the objective function to be minimized, and the model space is constituted by the infinite set of threshold vectors.

We found that after the completion of the process, the distribution of the event powers is more Gaussian, and then, more suitable for LSQ estimation; the corresponding residuals are consequently closer to a Rayleigh distribution. Physical consistency of the resulting TF has been tested by 1D inversion. The algorithm can, therefore, be combined with the MT remote-reference technique, and we found that it is effective to reduce the effects of artificial strong-power signal that can deteriorate the acquisitions. We present the successful application of this new technique to MT data collected over an East African Rift System geothermal area.

1. INTRODUCTION

Due to its inherent advantages, magnetotellurics (MT) has become the standard geophysical method for geothermal exploration since the '80s (Berktold, 1983). This technique exploits the low-amplitude variations of the natural magnetic field, produced by many natural sources. Its successful application for geothermal investigation arises from the low-cost, logistic effectiveness and high production rates, allowing to effectively depict the subsurface resistivity structure down to several kilometres depth.

However, as geothermal development proceeds on a global scale, a magnetotelluric investigation can involve densely populated and industrialised areas. In these zones, high-power artificial sources acting at a few specific frequencies, are more likely present. Since these signals can by persistent, robust methods can fail, and preliminary filtering can be ineffective. This hampers the applicability of MT in many areas or limits its reliability. The robust method can also fail since the high-power noise signal can constitute a high S/N portion of the data (see, e.g. Egbert, 1996, Weckmann, 2005).

A possible solution can be the manual selection of good data sections or frequency-domain events if the disturbance signal is easily detectable. In case this noise is persistent, this approach can be tricky or impossible, and therefore an automated scheme is preferable.

2. OUTLINE OF THE ALGORITHM

The rationale for the algorithm is that strong-power (respect to the natural EM signal) noise causes severe bias in the TF at particular frequencies, according to its origin. In industrialised areas, the main noise source comes from the power network, acting at a 50 Hz (or 60Hz) and some harmonics and sub-harmonics (Szarka,1988, Junge,1996). The pre-acquisition filters, embedded in

MT equipment, can be ineffective to eliminate this issue. Moreover, any filter will equally attenuate the natural signal to be analysed, causing an information loss.

The frequencies at which the TF is biased are immediately recognisable since it is dramatically sharpened. It is assumed that the smooth remaining portion of the TF is unbiased. The bias at these points can be removed by an inverse approach aiming at eliminating the outliers from the frequency domain events used for the impedance estimation. The roughness of the resulting TF is then reduced. The smoothness of the MT TF is often used as a quality indication (Jones, 1989), and is also artificially introduced by a-posteriori smoothing (e.g. Wannamaker, 1989), but this approach lacks physical consistency. It can also be part of estimation methods but implying the adoption of some arbitrary assumptions (e.g. Larsen, 1996).

The MT impedance single-station estimation by LSQ is given by (e.g. Chave, 1989)

$$Z = (E\ B^h)(E\ B^h)^{-1} \qquad (1)$$

where, **E** and **B** are frequency-dependent n X 2 (two-components) field matrices, where n is the number of observations; h denotes the Hermitian conjugate.

The assumptions to be made when applying (1) is that the errors are only affecting the E-field, their distribution is nearly-Gaussian and that they are independent. These conditions can be approached if a proper event selection is made before the LSQ estimate. To reduce the influence of the noise in the B channel, the Remote Reference technique is applied (Gamble et al., 1979); hereafter, we only deal with RR estimate, since we noticed from our experience that in the vast majority of the cases some noise affects the magnetic field acquisitions.

However, in our approach, the event selection is performed by applying power thresholds to the local EM field. This approach is for example used in GDS (Geomagnetic Depth Sounding) to prevent the influence of strong auroral electrojet field in Antarctic regions (Armadillo, 2001) and is somewhat analogous to the method by Jones (2002) for northern auroral zones.

The implemented inversion algorithm seeks for minimisation of the following functional

$$U(t) = ||\delta_R\ R|| + \mu\ ||\delta_\phi|| \qquad (2)$$

where, **R** is the p x 2 - matrix of the apparent resistivity, ϕ is the p x 2 - vector of the phase, and δ_R and δ_ϕ are the p x p difference matrices to be applied to the apparent resistivity and phase matrices used to compute their differences; p is the length of the estimation frequency vector. The factor μ is a trade-off between resistivity and phase smoothing. Variable *t* is a threshold vector. We only consider xy and yx - mode; therefore, the first column of matrix **R** or ϕ is referred to the xy-polarization, while the second one to the yx. Note that the minimisation of (2) aims at producing a smooth MT transfer function.

The frequency-dependent thresholds are automatically applied to the power of the electric field events until the maximum TF smoothness is reached. The set of all these thresholds form a p-vector *t'* that, from the classical inversion theory standpoint, constitutes the sought model. In other words, the model space in our algorithm is constituted by the infinite set of frequency-dependent power threshold vectors. The optimal model will, therefore, correspond to the threshold vector that will allow to exclude or minimise the influence of the outliers from the final LSQ estimate. We found that the optimisation is much more effectively carried out employing a derivative-free algorithm. We threfore used an unconstrained direct-search algorithm implemented in MATLAB®. The initial model of the inversion is usually chosen to compute the median or mean value of the electric field power of the event sets at the various estimation frequencies; this is computed separately for Ex and Ey.

## 3. APPLICATION TO DATA FROM GEOTHERMAL EXPLORATION

We applied our algorithm to a MT dataset from a geophysical survey carried out over the Kasitu geothermal field, Malawi (Fig.1). The data was acquired in the period June - July 2017, using a Remote Reference site located about 20 Km south of the survey area. The area is interested by the presence of a 50 Hz power line located along the main road; from our data analysis, we found that the stations lying along it are affected by noise up to a distance of about 700 m.

With the purpose to test the capabilities of our algorithm, we first contaminated by synthetic gaussian noise MT data gathered in an EM quiet site, located at about 3.5 km from the power line (station MT51, Fig.1). The noise was added to the Ex, Ey, Hx and Hy events at the frequencies of 57, 117 and 338 Hz. These estimation frequencies are the closest to the power line fundamental and its 3rd and 7th harmonics; the power line harmonics influence the estimation frequencies since the latter comes from a band-weighted average that comprises them.
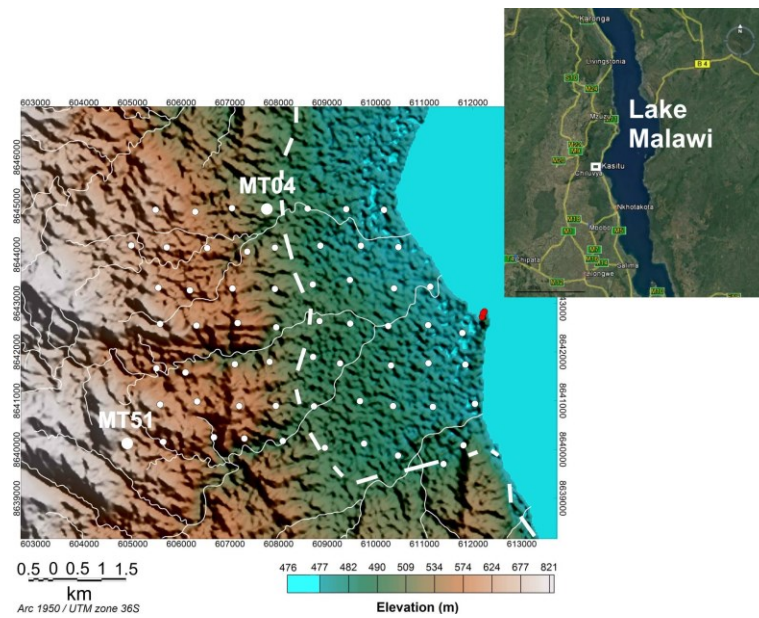
Figure 1. The Kasitu geophysical survey area. White dots indicate the MT stations. The dashed white line marks the main road, along which the power lines is located. Red dots mark the Kasitu hot springs.

The standard deviation of the noise signal was set to 1000 times the average signal. In Fig.2 are shown the Ex events at 57 Hz, after noise addition. It must be remarked that 80% of the events have been affected by artificial noise, simulating a persistent disturbance.
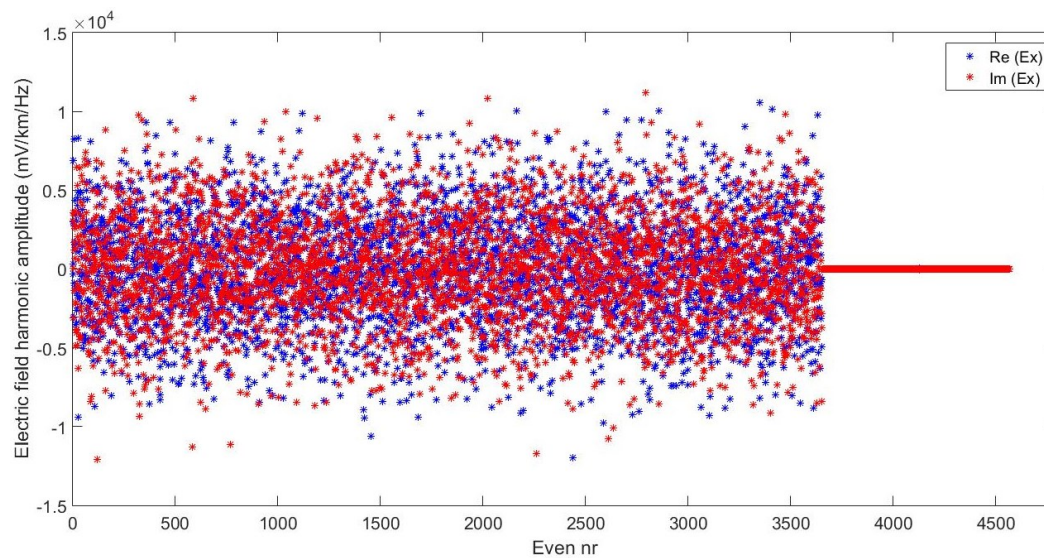

Figure 2. Example of data (Ex field) contaminated by synthetic gaussian noise.

Our inverse TF estimation was set to search for apparent resistivity and phase smoothing, using equal weight (μ=1). The inversion started from the average of the E - field and was stopped after 86 iterations; the frequency range was limited between 338 Hz and 1 Hz. The results are shown in Fig.3, where they are compared with a robust estimate (according to the Sutarno, 2008, algorithm); it can be observed that this latter fails to find an acceptable result, due to the fact that most of the data are contaminated by noise.
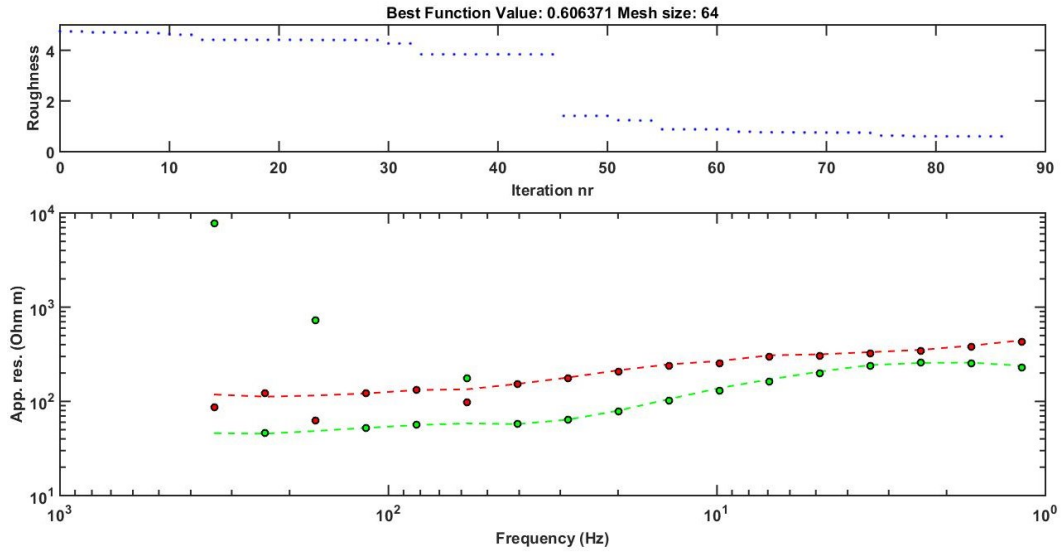
Figure 3. Smooth estimation of real data contaminated by synthetic noise. The smooth estimate is marked by dashed lines, the robust one by dots. Top: iteration progress.

Hereafter, we process the data from station MT04, lying at about 350 m from the power line (Fig.1). The used MT equipment recorded the EM data using three different sampling rates: 2400, 150 and 15 Hz. The noise is well evident in the 2400 Hz - sampling record, and much less in the 150 Hz; it is not visible in 15 Hz - sampling. Noise is ubiquitous in all channels except Hx. An example of the 2400 Hz band is shown in Figure 4.
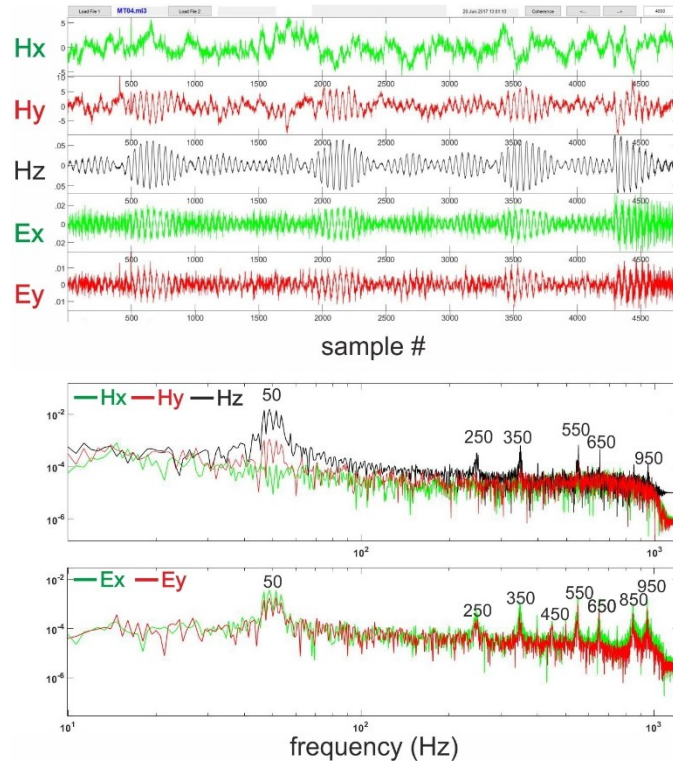
Figure 4. The EM signal at station MT04 (2400 Hz band). Top: time series, bottom power spectra.

Data shows strong and modulated 50 Hz noise. The inspection of other data windows shows that the noise is nearly continuous across the whole record length. Spectral analysis reveals the 50 Hz fundamental harmonic and the odd upper harmonics up to 950 Hz. The hodogram analysis (Fig.5) shows an E-polarization coherent with the orientation of the power line (about NNW). The H-

field hodograms indicate the quasi-verticality of the field. The strong polarisation shown by these diagrams indicates a predominant linear EM source.
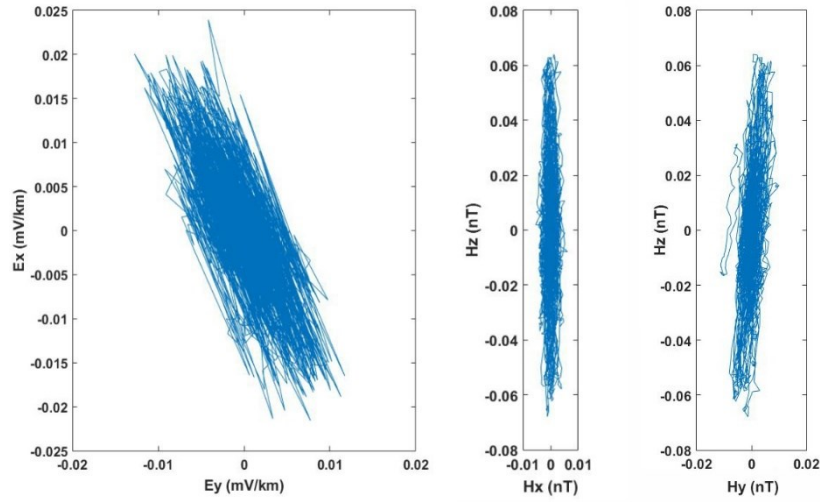
Figure 5. Hodograms of the EM signal at station MT04 (2400 Hz-band).

In Fig. 6, we show the results of our smooth inverse estimation, compared with the robust estimate. We adopted phase and apparent resistivity smoothing (with phase weight = 10) and Remote Reference (RR) estimate. The RR site was chosen at about 20 km south of the MT04 station. The initial model for the inversion was computed from the average E-field power of the event dataset. The inversion was stopped after 266 iterations.

As can be seen, the smooth estimation eliminates the noisy (sharp) points, both in the xy/yx apparent resistivity and phase data. Again, it can be noticed that the robust method failed to find an acceptable result since the power line noise is persistent. In fact, from the robust curves, it can be seen noise in the Z at the estimation frequencies of 57, 237 and 338 Hz; these frequencies are the closest to the fundamental, fifth and seventh harmonics of the power line signal.
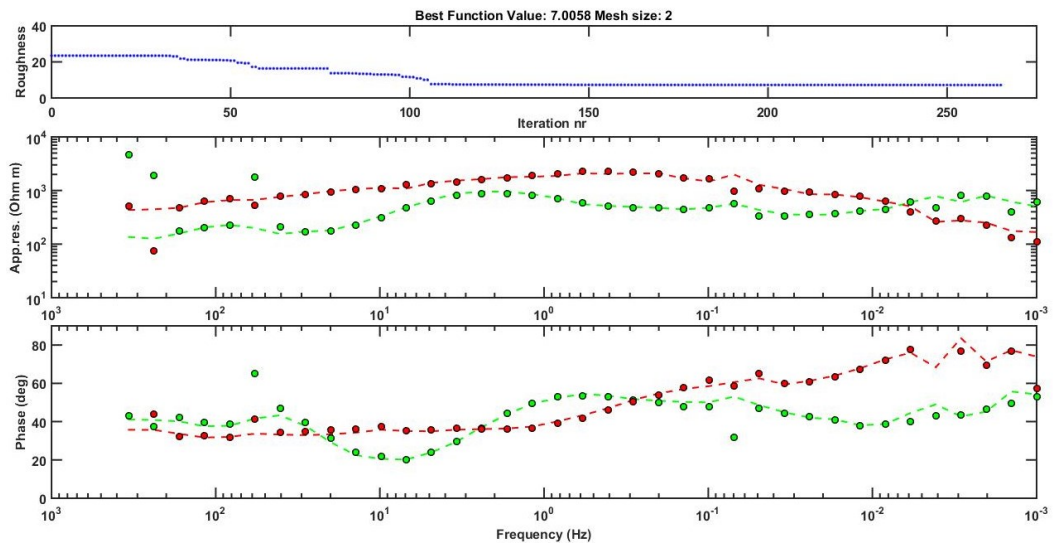
Figure 6. Results of the smooth transfer function MT estimation (dashed lines) for station MT04. The robust estimate is shown by dots.

From the analysis of the QQ (quantile-quantile) plots of the power of the Ex-events (Fig.7), it can be observed that after the selection process is completed, the distribution of the event powers are more gaussian, and then, more suitable to LSQ estimation (Fig.7, top); the corresponding residuals are consequently closer to a Rayleigh distribution (Fig.7, bottom).
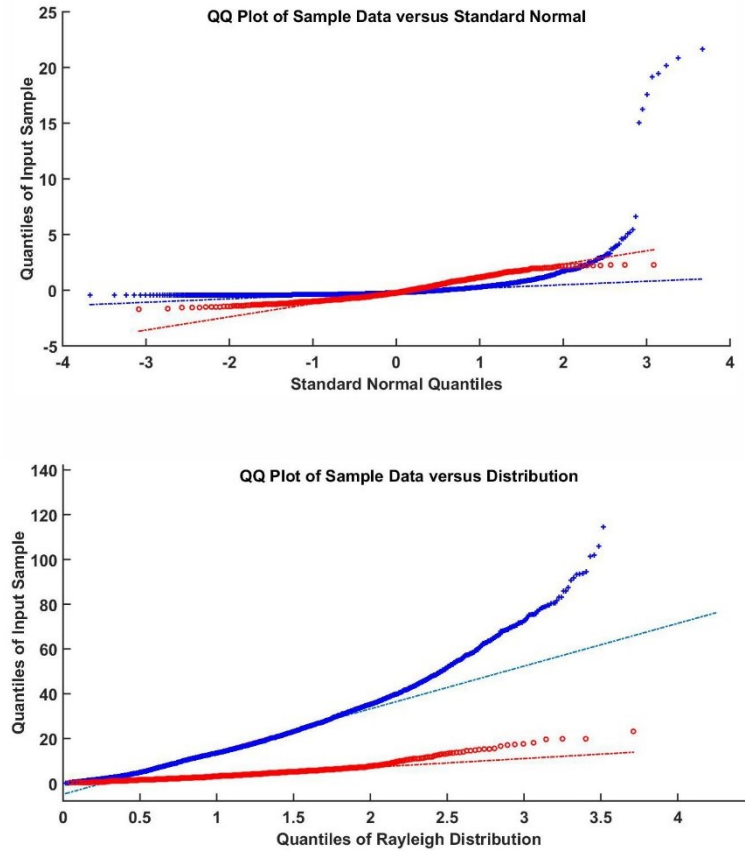
Figure 7. Ex power and residual QQ plots at 57 Hz: blue before smooth algorithm, red after it. Top Ex power, bottom Ex residuals. Data are more gaussian (or Rayleigh) distributed after event selection.

4. 1D MODELLING

With the aim to test the physical consistency of our smoothly estimated MT TF, we performed the 1D inversion of the effective impedance. Static shift factor to be applied to the MT apparent resistivity was estimated by joint inversion of effective MT phase and TDEM data and resulted to be 0.6. The results of the modelling are shown in Fig. 8. Considering the noise level, the inverted model explains reasonably well the data.
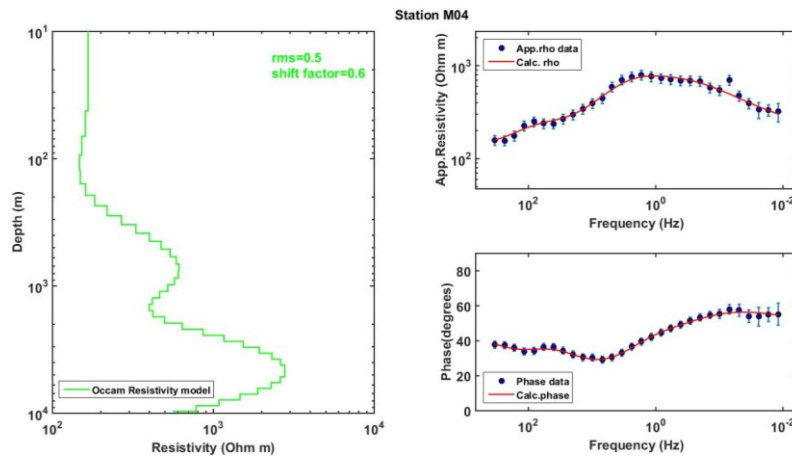

Figure 8. Occam 1D inversion of the smooth impedance for station MT04.

5. CONCLUSIONS

We have presented the capabilities of a new MT impedance estimation algorithm, conceived to obtain the smoothest possible TF through an inverse scheme. It has been successfully tested with synthetic noise applied to quiet MT station data, where 80% of the data was contaminated.

The algorithm demonstrated to be effective in eliminating ubiquitous and continuous power line noise at the base frequency (50 Hz), and its odd harmonics, at one geothermal survey site located in Malawi; the physical consistency of the obtained MT transfer function has been successfully tested by 1D inverse modelling.

Although we only applied our method to noisy data coming from an electric power line, we deem that it could be successfully applied to those cases where strong and persistent artificial noise sources are present in any survey area. This could aid the MT exploration even in areas inaccessible so far, and therefore it should be considered as a promising tool for the further development of geothermal energy.

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