

SEPARATING INTRINSIC FROM SCATTERING SEISMIC WAVE ATTENUATION FROM FULL WAVEFORM SONIC LOGS IN A GEOTHERMAL FIELD

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ABSTRACT

Elastic waves attenuate in the earth due to scattering and absorption. The latter can be linked to fluid movement and is of the utmost importance to the production of a geothermal field. However, it is hard to separate scattering from intrinsic attenuation. Our approach is to use the full elastic waveform from borehole sonic logging, which consists of a coherent part, and incoherent signal produced by the scattered waves (coda). Based on the radiative transfer theory, the coherent energy is affected by the elastic wave attenuation due to both scattering and intrinsic attenuation, while scattering can provide a gain term in the incoherent energy. Here, we quantitatively analyze these intensities to independently estimate the quality factor due to scattering and absorption from full waveform sonic logs in a geothermal field.

1. INTRODUCTION

The analysis of elastic waves in the earth is often focused on estimates of the travel time (phase) of the first arriving compressional and/or transverse waves. However, seismologists now also analyze wave amplitudes to estimate the properties of the subsurface. One way to extract rock property information is to analyze the decay of seismic amplitude with distance; i.e., the loss of elastic energy due to elastic wave attenuation. Scattering attenuation is caused by heterogeneity in the earth, in the form of different rock materials, or in the presence of fractures. Intrinsic attenuation, or absorption, can be due to fluid movement as a result of a passing seismic wave. In field measurements, separating the loss of energy due to absorption versus scattering is difficult.

Wave attenuation is commonly described through the Quality Factor (Q) or its inverse (Q^{-1}) (Knopoff, 1964):

$$\frac{1}{Q} = \frac{\alpha v}{\pi f} , \quad \alpha = \frac{1}{x_2 - x_1} \ln \frac{A(x_1)}{A(x_2)} \quad (1)$$

where x_2 and x_1 are two different positions, $A(x_1)$ and $A(x_2)$ are the amplitudes measured at those positions and v and f are the velocity and frequency of the wave, respectively. The inverse of the quality factor provides a means of quantifying the dissipation of energy of the wave in a whole cycle of oscillation. The main factors affecting the value of Q summarized by Johnston (1981) and Müller et al. (2010) are: wave frequency, pore and confining pressures, fluid saturation, strain amplitude, fractures and rock composition (e.g. the degree of pore connectivity and mineralologic

alteration). How these factors affect elastic wave propagation in rocks has been investigated in the laboratory for several decades (Birch (1960); Kern (1978); Toksöz et al. (1979); Batzle and Wang (1992); Punturo et al. (2005); Adam et al. (2009); Batzle et al. (2014)). Johnston et al. (1979) reviews some of the mechanisms acting at ultrasonic frequencies, concluding that friction, fluid flow, viscous relaxation and scattering are dominant. Müller et al. (2010) summarize the wave-induced fluid flow mechanisms (models) in the context of seismic wave attenuation. Understanding which are the main fluid and rock properties that control seismic wave attenuation is complicated. In deciding which attenuation mechanisms apply to field observations of Q, we would like to separate the scattering attenuation (Q_s) from absorption (Q_a).

Different methodologies have been proposed to estimate total attenuation from sonic logs (e.g. Cheng et al., 1982; Dasios et al., 2001; Parra et al., 2007). The most common methodology to estimate total Q from waveform data is by using spectral ratios of P-wave arrivals (Toksöz et al., 1979). However, Parra et al. (2007) point out that wave reflections and scattering can introduce oscillations in the amplitude spectra of the waveform, making it difficult to estimate Q from spectral ratios. In either case, the estimate of Q is the sum of scattering and intrinsic Q. Instead, We use elastic full waveform sonic data to estimate interval quality factors (Q_s and Q_a) with depth in a borehole. Our methodology focused on studying the energy produced by guided waves, and their scattering (i.e. coda). We first present a brief description of the full-waveform logging tool and common datasets. Next, we summarize the theory behind the radiative transfer theory. Finally, we present estimates of Q_s and Q_a and a preliminary interpretation for two wells in the Ngatamariki Geothermal Field, New Zealand.

1.1 Radiative transfer theory

A wave is a perturbation of varying amplitude and phase in space and time. This perturbation, when performed over many realizations over the same medium, reveals systematic and fluctuating parts of the field; the coherent and incoherent field respectively. The square of the average wavefield $u(t)$ is known as the coherent intensity: $I_c = \langle u(x, t) \rangle^2$, whereas the average of the square of the wave fields is the total intensity $I_t = \langle u^2(x, t) \rangle$ (Ishimaru, 2013). The incoherent intensity of the field is the difference of the aforementioned intensities $I_i = I_t - I_c$. Radiative Transfer Theory describes the spatial and temporal dependence of the total intensity of seismic energy radiation in a particular direction (Paasschens, 1997). A quantitatively estimate of Q_a and Q_s offers an opportunity to identify sections where fluid movement is dominant (van Wijk, 2003). The Radiative Transfer Theory provides an opportunity to

separate scattering attenuation and absorption from full waveform log data based on the decay of the coherent and incoherent intensities of Stoneley waves in the borehole. The coherent ($C(x, t)$) and incoherent ($I(x, t)$) intensities according to the Radiative Transfer model in one dimension derived in Van Wijk (2003) and Haney et al. (2005) are:

$$I_c(x, t) \propto \exp(-\alpha vt) \delta(x - vt), \quad (1)$$

$$I_i(x, t) \propto \exp(-\alpha vt) \left(I_0(\eta) + \sqrt{\frac{vt+x}{vt-x}} I_1(\eta) \right), \quad (2)$$

where $\alpha = \left(\frac{1}{l_a} + \frac{R}{l_s} \right)$ and $\eta = \frac{R}{l_s} \sqrt{(vt)^2 - x^2}$ with l_a the absorption mean free path, R/l_s the back-scattering cross-section (R), l_s the scattering mean free path, v the group – or energy – velocity, and t and x equal time and offset, respectively. I_0 and I_1 are the zero-th and first-order modified Bessel functions, and f is the frequency of the wave. In the following, we will find values of the scattering and absorption mean free paths that best fit the intensity data. Then, these mean free paths are related to the more familiar:

$$Q_a = \frac{2\pi f l_a}{v}, \quad Q_s = \frac{2\pi f l_s}{v} \quad (3)$$

The Radiative Transfer Theory is implemented following a simple scheme. A common-offset section (ensemble) over a depth interval of interest is chosen and traces are stacked. Within this interval we estimate the total, coherent and incoherent intensity. The group velocity of the Stoneley wave for the ensemble stack is estimated from the coherent intensity of the 8 receivers. The coherent intensity and the incoherent intensity are fitted using equations 1 and 2 to estimate Q_a and Q_s as a function of depth in the borehole.

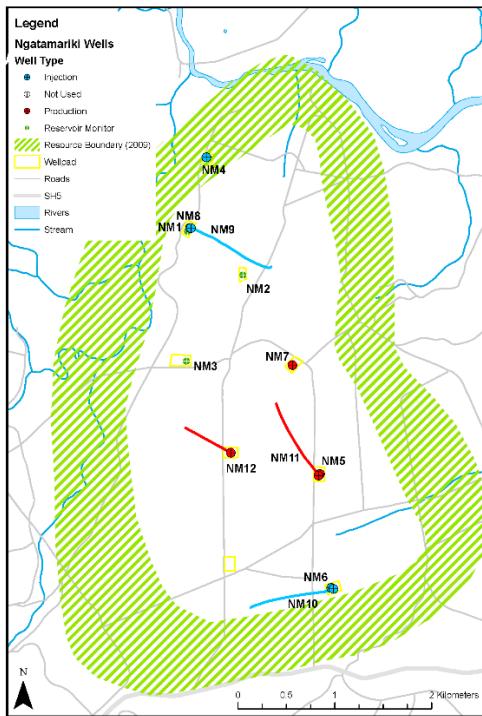


Figure 2 shows an ensemble of waveforms. One can clearly observe a coherent arrival of the Stoneley wave, which decays with offset. For each offset, the Stoneley wave is followed by scattered energy. The bottom panel displays an ensemble of 20 constant-offset traces from the first receiver.

The blue lines in the panels of Figure 3 are the total, coherent and incoherent intensity for the ensemble of waveforms in Figure 2. The red lines are the best fits to the different intensities, where a value of $R = 0.5$ was assumed for the backscattering cross-section (R); this implies for the 1D model assumed here that energy transmits and reflects equally at the scatterers within the ensemble. The group

velocity v of the Stoneley arrivals is estimated from the move-out of the peak of the total intensity as a function of source-receiver offset. From the fits shown in Figure 3, values of the absorption mean free path ($la = 1$ m) and the scattering mean free path ($ls = 0.55$ m) were estimated, which result in values of $Q_a = 59$ and $Q_s = 33$ respectively.

Figure 4 shows the estimated values of Q_a and Q_s for the well NM8, which we believe correlate with geology. For example, Q_a estimates are lower in the zones of washouts. A decrease in Q_a (i.e., stronger attenuation) between 1390 m and 1405 m is accompanied by a decrease in resistivity. This is likely indicating a region of favorable mobility for fluids.

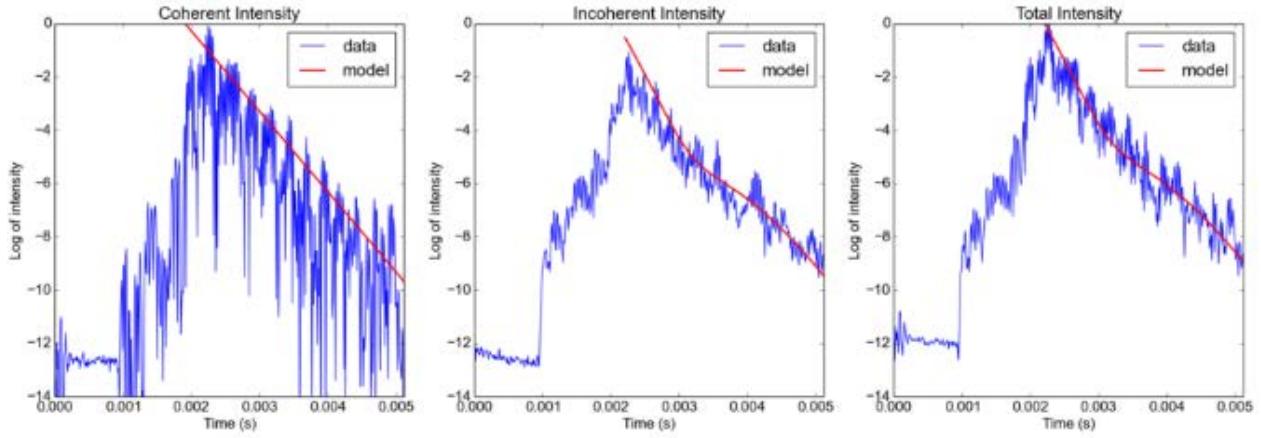


Figure 3: Wave intensities calculated from the ensemble of traces shown in Figure 2. From left to right: coherent, incoherent and total intensity. The values of Q_a and Q_s obtained for this fits are 59 and 33, respectively. The absorption mean free path (la) is 1 m while the scattering mean free path (ls) for a back-scattering cross-section $R = 0.5$ is 0.55 m.

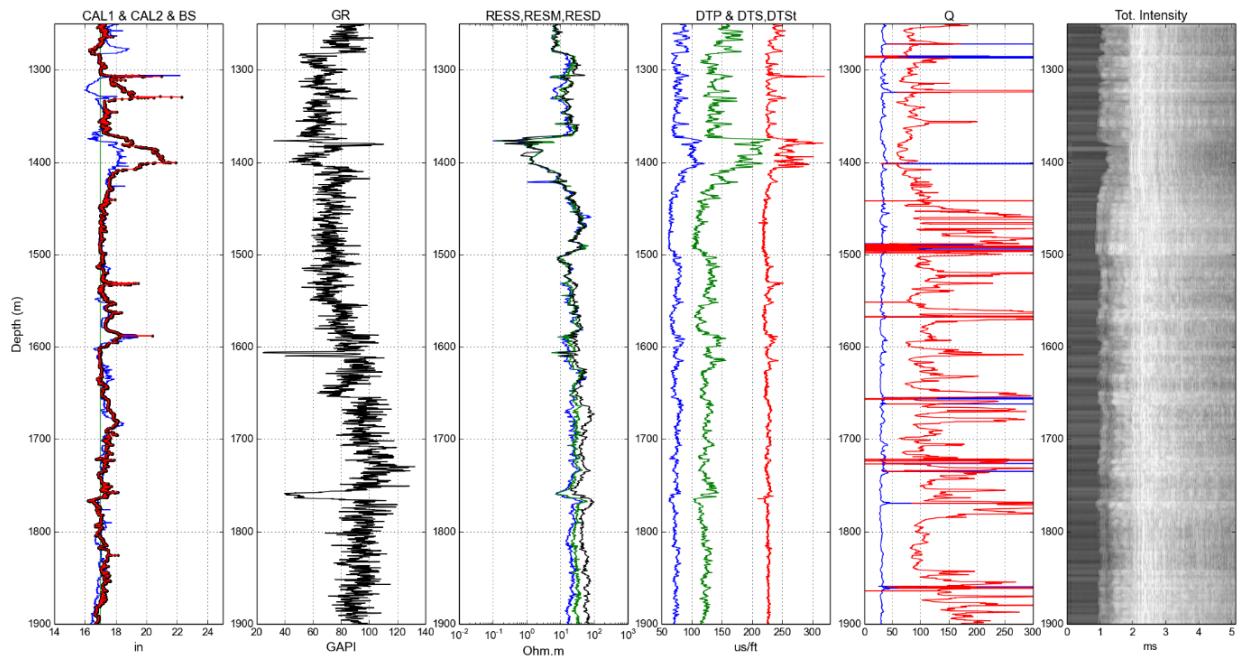


Figure 4: Geophysical well logs of the well NM8. The wash-out areas are those where the caliper logs read a greater borehole diameter than the bit size (17 in). The slowness logs correspond to the P-wave (DTP), S-wave (DTS) and Stoneley wave (DTSt). GR is the gamma ray log, RESS, RESM, RESD are resistivity logs. Q_a (red) and Q_s (blue) are estimated from an ensemble of 20 first receivers using the monopole source data.

Below this, estimates of Qa show an abrupt increase (lower attenuation) and higher variability. Geologically, this area corresponds to a welded ignimbrite. In this section, the resistivity increases, indicating less porosity and hence a higher level of compaction. The effect of the lithologies and their different levels of compaction and alteration must be evaluated in detail. Lower values of Qs than Qa seem to indicate that most of the attenuation is probably due to scattering in the borehole. The scattering attenuation estimates Qs show also less variability than Qa. The total value of Q is given by the combination of absorption (Qa) and scattering (Qs); when scattering is as strong as shown here, the absorption component related to fluids is almost completely masked. The separation of quality factors achieved by the radiative transfer model appears to overcome this difficulty.

2.2 Estimations on Well NM10

The logged part of well NM10 corresponds to the Ngatamariki Andesite. This andesite has a high number of conductive fractures (Halwa, 2012). Figure 5 shows the correlation between absorption (Qa) and FMI fracture density interpretation for the top section of the andesite (this section has the highest quality sonic data). The plot shows only conductive fractures with no halo, which are interpreted as open or clay-filled fractures (Halwa, 2012). A preliminary correlation between low absorption (high attenuation) and higher fracture density can be observed. Open fractures in rocks are responsible for the losses in wave energy due to pore pressure disequilibrium created by the passing wave (Pride et al., 2004).

High Qa (low attenuation) overall correlates to sections where fracture density is low. Although the correlations between Qa values and fracture density is generally strong, a lack of correlation in some parts can be due to 1) clay-filled fractures that contribute to the fracture density would not affect Qa, or 2) FMI images have a lower resolution of 5 mm, however these micro-fractures will still affect the flow properties and attenuation of waves. Although the technique presented here has been applied to volcanic rocks, we believe this methodology and our findings can be equally applied to carbonate fractured rocks and/or high permeable sandstone reservoirs.

3. CONCLUSIONS

The estimation of a separate quality factor due to absorption and scattering is possible from the intensities of the radiative transfer model. The quality factor for absorption (Qa) appears to be sensitive to the different welding levels and wash-out zones of the pyroclastic deposits in well NM8A. The scattering quality factor (Qs) shows less variability through the well.

In well NM10 there is partial correlation between density of fractures and Qa. The types of fractures (opened or closed) and the size of the ensembles are important factors to consider for further improvement of the estimates.

The interpretation of the mean free paths in terms of the geological features is a pending task. Also the role of the back-scattering cross section must be evaluated in detail.

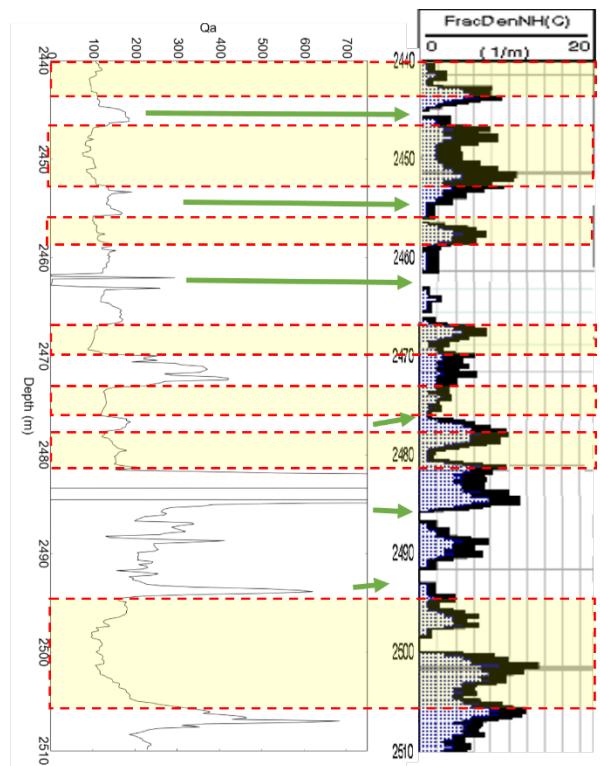


Figure 5: Preliminary interpretation of absorption Q on the upper andesite section at Ngatamariki (Well NM10). Fracture density log from (Halwa, 2012). The dashed square areas show the matches between the variations of Qa with the fracture density log.

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