

ISOENTHALPIC FLASHING POINT COMPRESSIBILITY OF GEOTHERMAL FLUIDS WITH LOW CO₂ CONTENT

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SUMMARY-Noncondensable gases in geothermal fluids have major effects on the behavior of the reservoir and fluid flow. The most common and dominant noncondensable gas in geothermal fields is carbon dioxide. Therefore effects of the CO₂ content on the flow characteristics and thermodynamic properties must be known. In this study the compressibility of the geothermal fluids containing low dissolved CO₂ at flashing point is formulated for isoenthalpic phase change. The compressibility called as isoenthalpic flashing point compressibility can be calculated with well-known parameters such as saturated water and steam densities, steam pressure and Henry's constant for CO₂. New easy to use graphs to estimate the compressibility for such systems are presented. Correction for ionic strength of the brine is also considered. The practical use of the compressibility is illustrated by using a material balance method to estimate the fluid content of a geothermal reservoir.

1. INTRODUCTION

The water produced by geothermal wells most frequently contains noncondensable gases and dissolved solids. They have considerable effects on the behavior of the reservoir and fluid flow. In its natural state, the partial pressure of the noncondensable gas causes the reservoir to flash at a higher pressure than does pure water. The presence of noncondensable gases in produced fluid dominates the transport and thermodynamical properties of the flow. The most common and dominant gas in geothermal fields is carbon dioxide. The studies (Sutton (1976), Parlaktuna (1988), Alkan and Satman (1990), Ugur (1997)) show that small differences in the CO₂ content of the reservoir fluid causes significant changes in the pressure, enthalpy and gas content of production fluid.

In general the geothermal fluids are brine-CO₂ solutions with relatively low dissolved solid and noncondensable gas content. Thermodynamic properties and the pressure-volume- temperature (pVT) behavior of these type solutions have been studied experimentally and theoretically (Ellis and Golding (1963), Edwards et al (1978), Jin and Donhoue (1988), Enick and Klara (1990), Satman and Alkan (1990), Crovetto (1991), Joyce and Holloway (1993), Oddo and Tomson (1994), Millero (1995), Ugur et al (1996)). Some of these studies presented the models which vary according to the parameters such as temperature, pressure and ionic strength

of the solutions. Mostly they can be employed to represent the two-phase domain characteristics of the geothermal fluids.

In this paper, the compressibility of brine-CO₂ solutions at the flashing point, that is one of the most important thermodynamic properties, is formulated with the known parameters for the isoenthalpic phase change and called as isoenthalpic flashing point compressibility.

Ionic strength effect on the compressibility is calculated and presented. It is also demonstrated by a case study that isoenthalpic flashing point compressibility can be used for estimating initial fluid volume of a geothermal reservoir.

2. ISOENTHALPIC FLASHING POINT COMPRESSIBILITY

Compressibility of the brine-CO₂ solutions especially at the flashing points depends on gas CO₂ compressibility, because the vapor phase of geothermal fluid is composed of only gas CO₂ under these conditions. Figure 1 shows the pressure-enthalpy- temperature diagram for a given brine-CO₂ solution (Ugur, 1997).

It reveals extremely different phase behavior at low steam quality values as compared to the enthalpy diagram for pure water system. As

seen in Fig. 1 one can say that brine-CO₂ solutions show isenthalpic behavior during the phase change at relatively low steam quality values (up to 3 wt %). Using this characteristic, the compressibility for a brine-CO₂ system at flashing point conditions can be formulated at fixed temperature (T) as follows :

$$c_c = \frac{K_H \rho_w}{\rho_s} \frac{18 p_s}{44 p_{CO_2}} \quad (1)$$

Where:

- c_c : Isoenthalpic flashing point compressibility, 1/Pa
- K_H : Henry's constant, 1/Pa
- P_s : Steam pressure at T, Pa
- P_{CO_2} : Partial pressure of CO₂ at T, Pa
- ρ_w : Water density, kg/m³
- ρ_s : Steam density, kg/m³

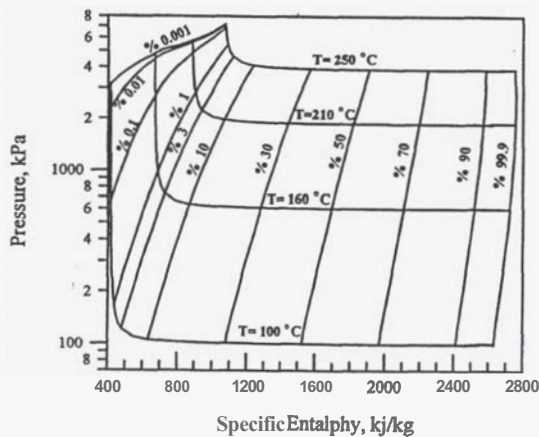


Figure 1 Pressure-enthalpy-temperature diagram for brine - CO₂ solution with 0.05 M ionic strength and 1.5 wt % initial dissolved CO₂. (Percentage values in two-phase region represent steam quality) (Ugur, 1997).

The derivation of Equation 1 is given in Appendix A. Values of densities and Henry's constant were calculated using the pVT model presented by Ugur (1997). For Henry's constant pVT model employs Satman's (1990) correlation which was developed using mainly Ellis-Golding (1963) experimental values. This correlation is valid up to 300 °C temperatures and 2 M values of ionic strength (M). Furthermore densities of pure water and steam

and steam pressure can be taken from steam tables.

Figure 2 gives the isenthalpic flashing point compressibility values as a function of the CO₂ concentration and temperature for pure water-CO₂ solutions. Range of temperature and CO₂ concentration of the solutions were chosen considering geothermal reservoir conditions in Turkey. As seen in Fig. 2 the lower the dissolved CO₂ concentration in solution is, the greater the compressibility of the solution becomes.

In Fig. 3 ionic strength effect of the solutions on compressibility is given as a function of temperature. Fig. 3 gives the ratio of the Compressibility of brine-CO₂ solutions (c_c) to the compressibility of water-CO₂ solutions (c_c (M=0)). The values for c_c (M=0) are taken from Fig. 2. Note that presence of the dissolved solids in brine lowers compressibility. Using Fig. 1 and 2, one can estimate isenthalpic flashing point compressibility for brine-CO₂ solutions. For example, the compressibility of the brine- CO₂ solution with 0.5 M ionic strength and 1.2 wt % CO₂ content at 200 °C can be found as follows. First, from Fig. 2 the compressibility value for water-1.2 wt % CO₂ solution corresponding to the given temperature is read to be 8.0×10^{-5} 1/kPa. Then, from Fig 3, the ratio (c_c/c_c (M=0)) corresponding to the given ionic strength and temperature is read to be 0.54. Finally the last value is multiplied by the compressibility value read from Fig. 1. The result, 4.32×10^{-5} 1/kPa, is the isenthalpic flashing point compressibility of the given brine- CO₂ solution.

3. PRACTICAL USE OF ISOENTHALPIC FLASHING POINT COMPRESSIBILITY

Isoenthalpic flashing point compressibility can also be used to estimate the initial fluid volume of a geothermal reservoir where isoenthalpic phase behavior exists, as illustrated below:

Consider a geothermal reservoir in which there is a production and water recharge, a simple volumetric balance similar to the one for volumetric oil reservoirs (Craft and Hawkins, 1959) can be written as follows:

$$\frac{B_w W_p - W_e}{(c_f + c_e) \Delta p} = V_{pi} \quad (2)$$

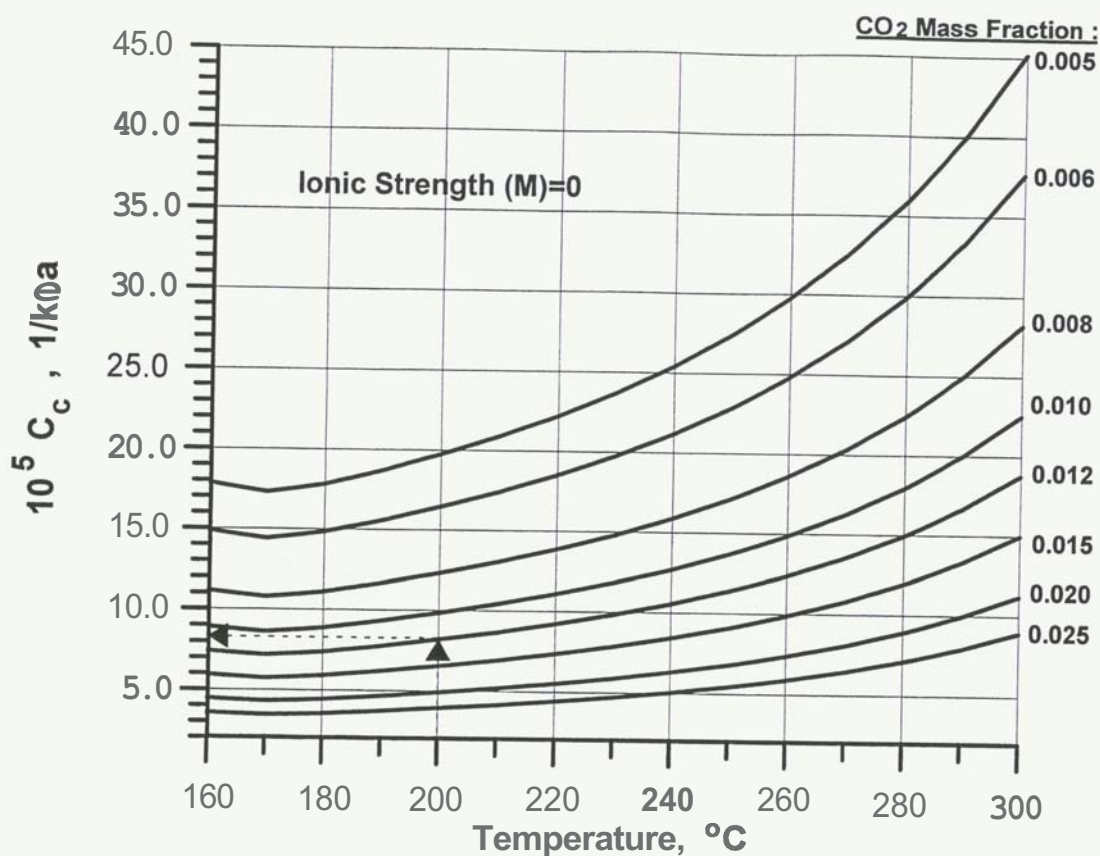


Figure 2 Isoenthalpic flashing point compressibility for various water-CO₂ solutions

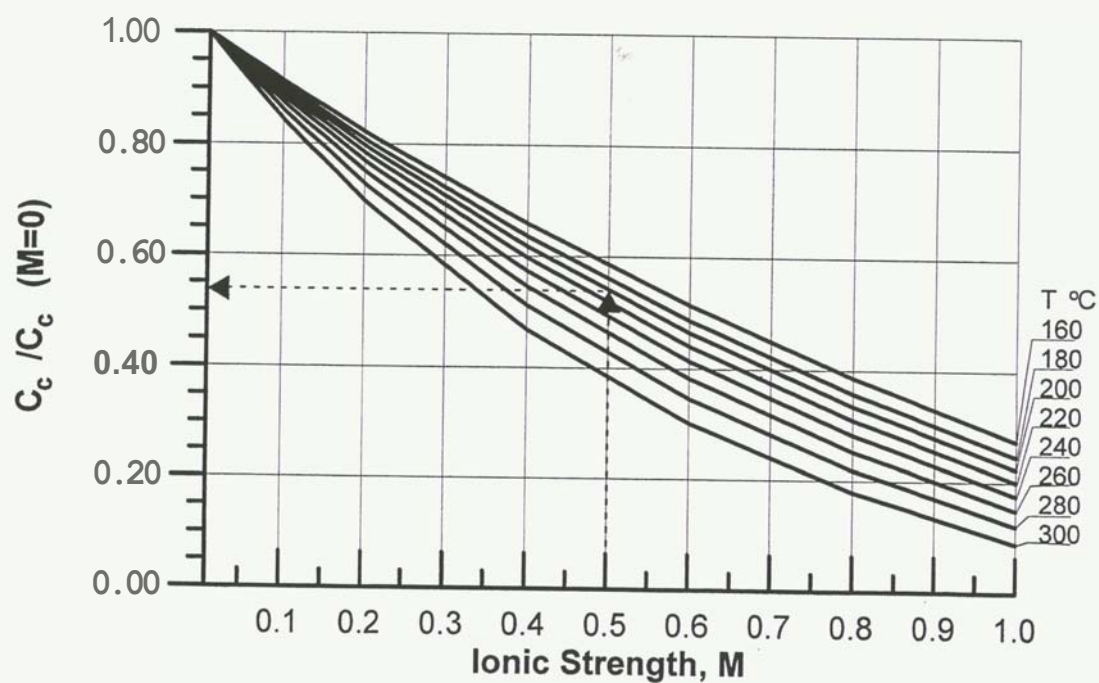


Figure 3 Ionic strength effect on the compressibility of brine-CO₂ solutions

Where

- V_{pi} : Initial fluid volume,
 $B_w W_p$: Produced volume,
 W_e : Volume of water influx into
the reservoir,
 c_f : Formation compressibility,
 A_p : Pressure drop as a result of
production.

Neglecting the formation compressibility, since its magnitude is much smaller than the isenthalpic flashing point compressibility, then gives the following equation:

$$V_{pi} = \frac{1}{c_e} \frac{\Delta V}{\Delta p} \quad (3)$$

Where: $\Delta V = B_w W_p - W_e$

Equation 3 indicates that the initial pore volume of a geothermal reservoir can be estimated if pressure drop, A_p , is known as a function of volume change in the system, ΔV .

Applicability of Equation 3 is demonstrated by using the observed production behavior of the Kizildere geothermal field. The modelling study of the field (Alkan and Satman, 1990) and measured reservoir pressure- cumulative production data clearly show the isenthalpic two-phase behavior. During the time period between 1991 and 1995, the average production rate from the field was 7 million ton per year and natural water influx into the reservoir was estimated to be 550 ton/hour (MTA, Satman et al. 1996). Well KD-7 was chosen to be the representative average well for the field because of its central location in the reservoir and its reliable pressure data measured during the two-phase production period. Data obtained from this well are 200 °C bottom hole temperature and 8.1 kPa pressure drop per 10^6 ton fluid production, and geothermal fluid with 1.2 wt % initial dissolved CO_2 and ionic strength of 0.07 M (Satman et al. (1996), Tan (1984)).

Using the representative data in Figs. 2 and 3, flashing point compressibility, c_e , is determined to be 7.6×10^{-5} 1/kPa. Fluid volume change in reservoir, ΔV , is calculated using the natural water influx and production values. Substituting the respective values into Equation 3, the initial fluid volume of the Kizildere geothermal field is obtained to be 603 million cubic meters. This checks perfectly well with

the initial estimate of the reservoir fluid volume of 600×10^6 cu m (UN Report, 1974).

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Appendix A -Derivation of Isoenthalpic Flashing Point Compressibility

The compressibility is defined as the change in volume per unit volume per unit change in pressure, or

$$c = -\frac{1}{V} \frac{dV}{dp} \quad (A-1)$$

The compressibility resulting from the carbon dioxide can be written similarly to Equation A-1 as:

$$\frac{\Delta V}{V} = c_c \Delta p_{CO_2} \quad (A-2)$$

The volume changes when CO₂ leaves the water solution. Hence:

$$\frac{\Delta V}{V} = \frac{(\Delta m_{CO_2})_1}{\rho_{CO_2}} \rho_l \quad (A-3)$$

The amount of the CO₂ in the liquid phase is small and neglected in the liquid density, that is:

$$\rho_l = \rho_w \quad (A-4)$$

By using Equations A-2, A-3 and A-4 we can write for the compressibility:

$$c_c = \frac{(\Delta m_{CO_2})_1}{\rho_{CO_2}} \rho_w \frac{1}{\Delta p_{CO_2}} \quad (A-5)$$

Henry's law is employed to give

$$(\Delta m_{CO_2})_1 = K_H \Delta p_{CO_2} \quad (A-6)$$

Substituting Eq. A-6 into Eq. A-5 results in the final equation for the isoenthalpic flashing point compressibility for brine-CO₂ solutions:

$$c_c = \frac{K_H}{\rho_{CO_2}} \rho_w \quad (A-7)$$

Assuming

$$\frac{\rho_s}{\rho_{CO_2}} = \frac{18}{44} \frac{P_s}{P_{CO_2}} \quad (A-8)$$

then isoenthalpic flashing point compressibility is obtained as follows:

$$c_c = \frac{K_H \rho_w}{\rho_s} \frac{18}{44} \frac{P_s}{P_{CO_2}} \quad (A-9)$$